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16.485: VNAV - Visual Navigation for Autonomous Vehicles

Luca Carlone

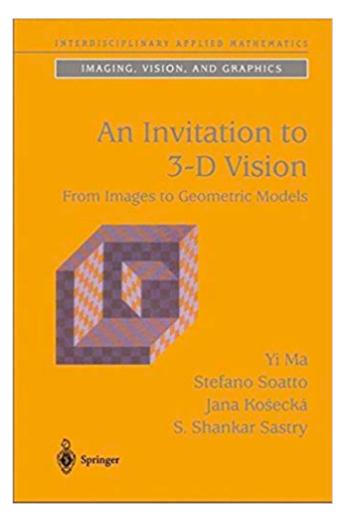


Lecture 14: 2-view Geometry



Today

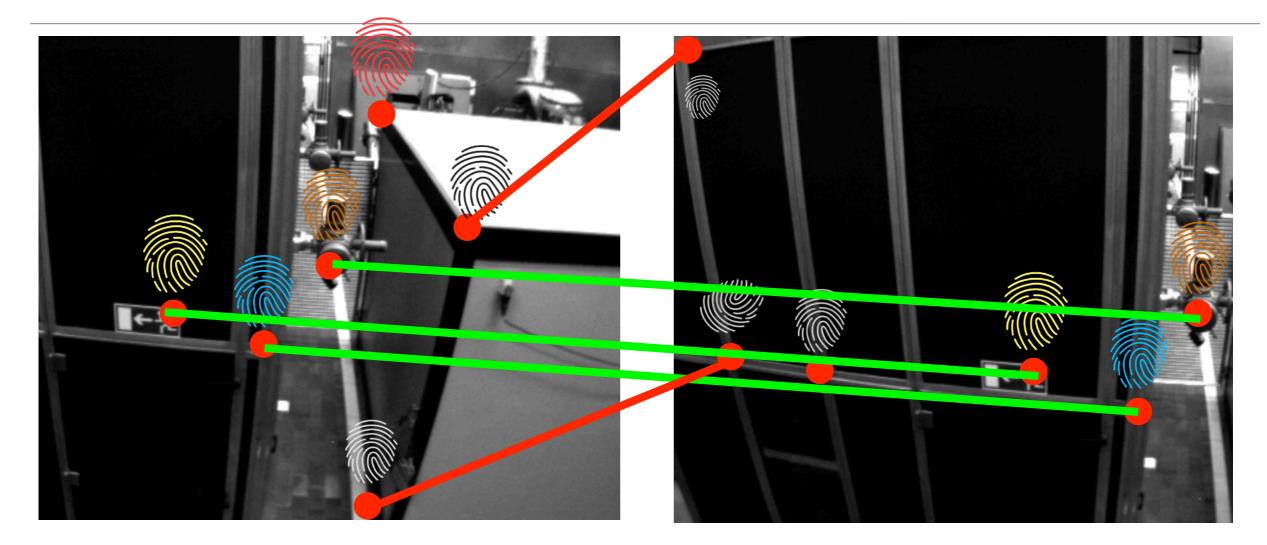
• 2-view geometry



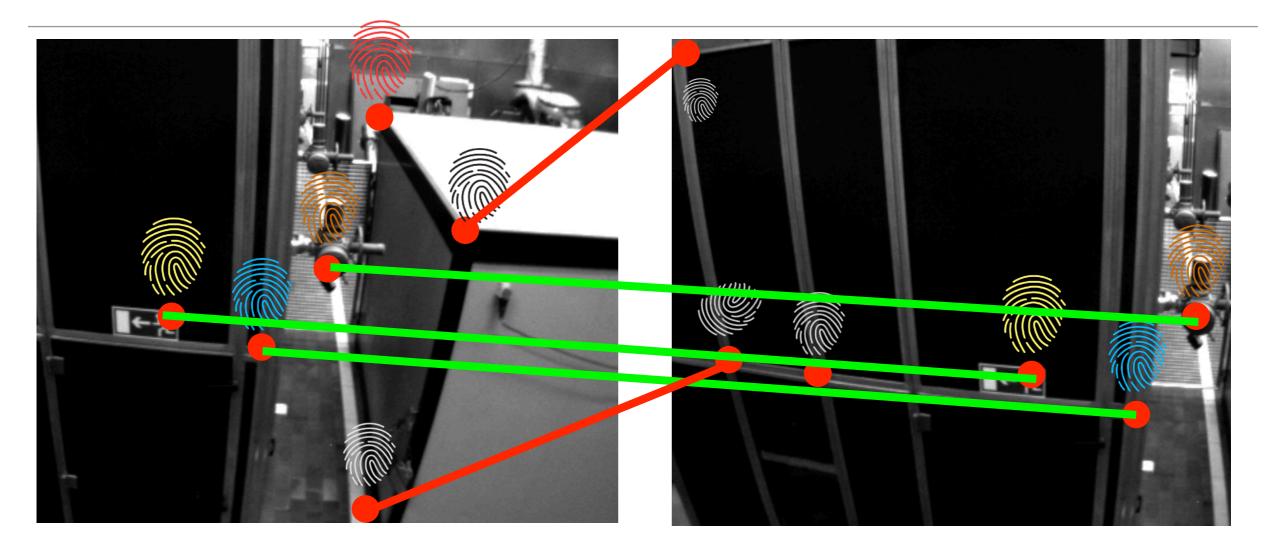
Chapter 5

Reconstruction from Two Calibrated Views

Recap: Point Correspondences

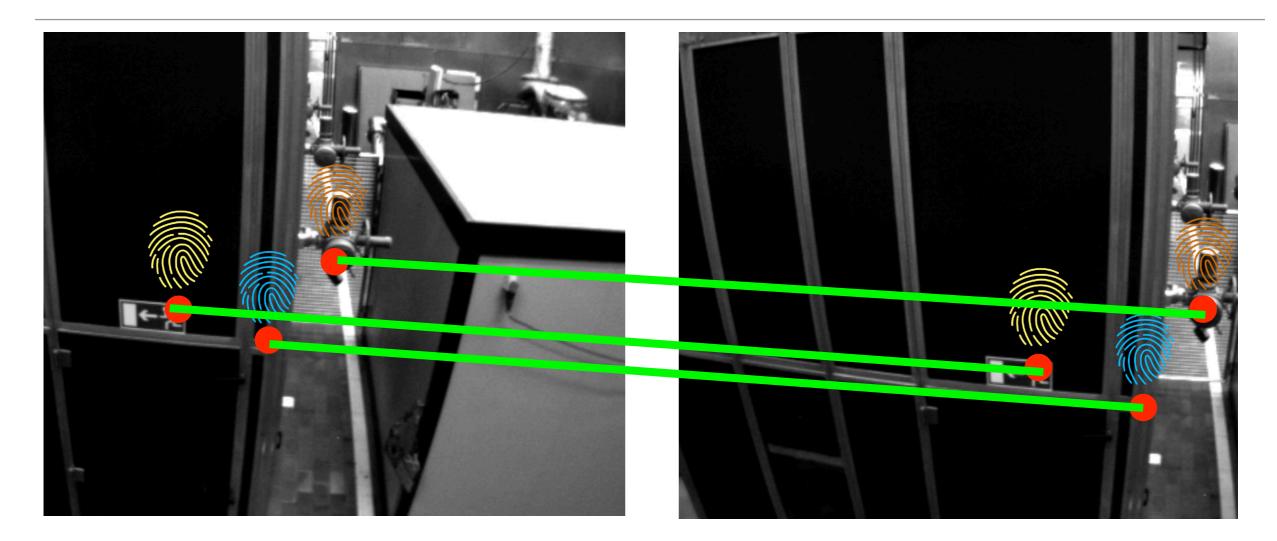


2-view Geometry



Question: can we estimate the motion of the camera between *I*₁ and *I*₂ using pixel correspondences?

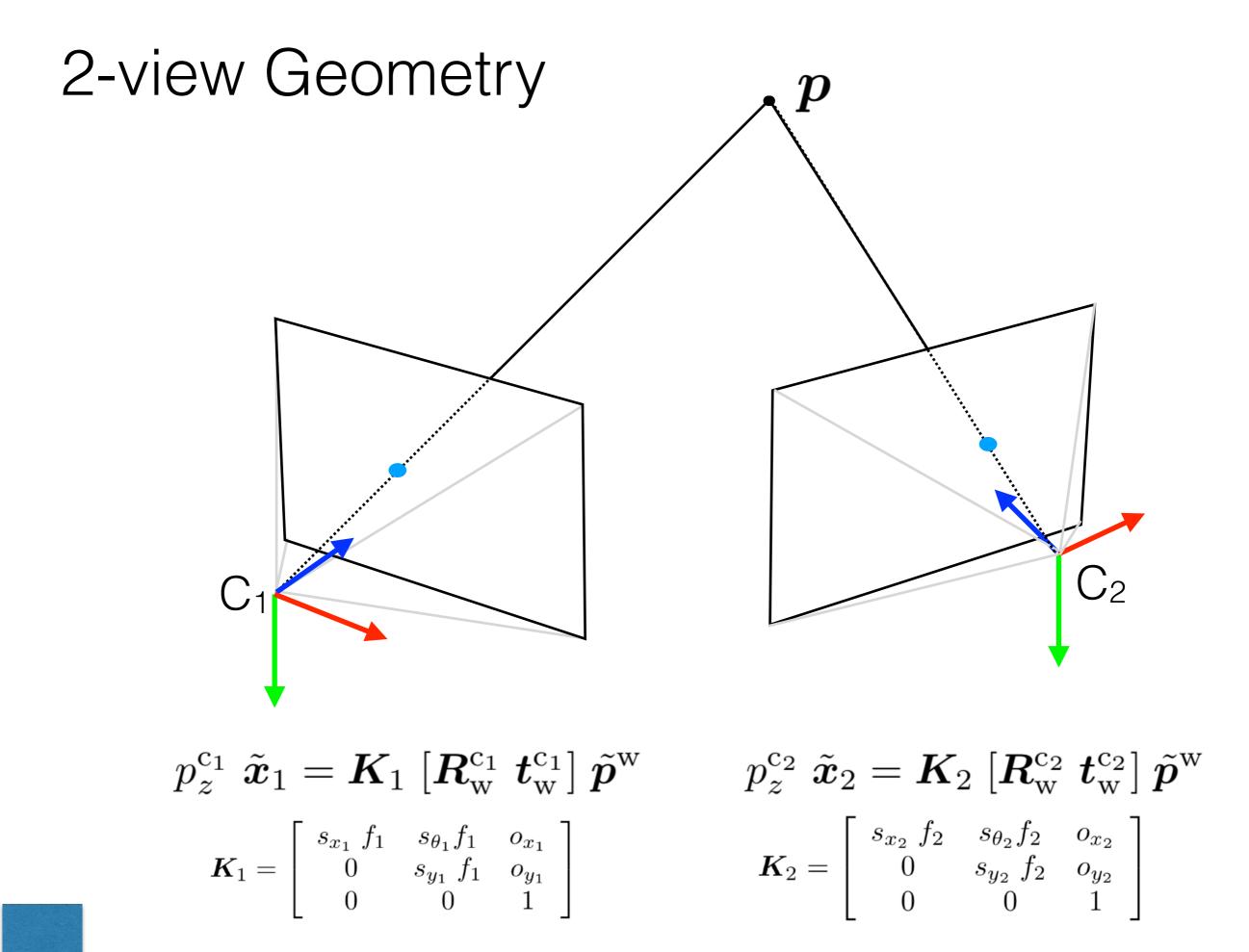
2-view Geometry

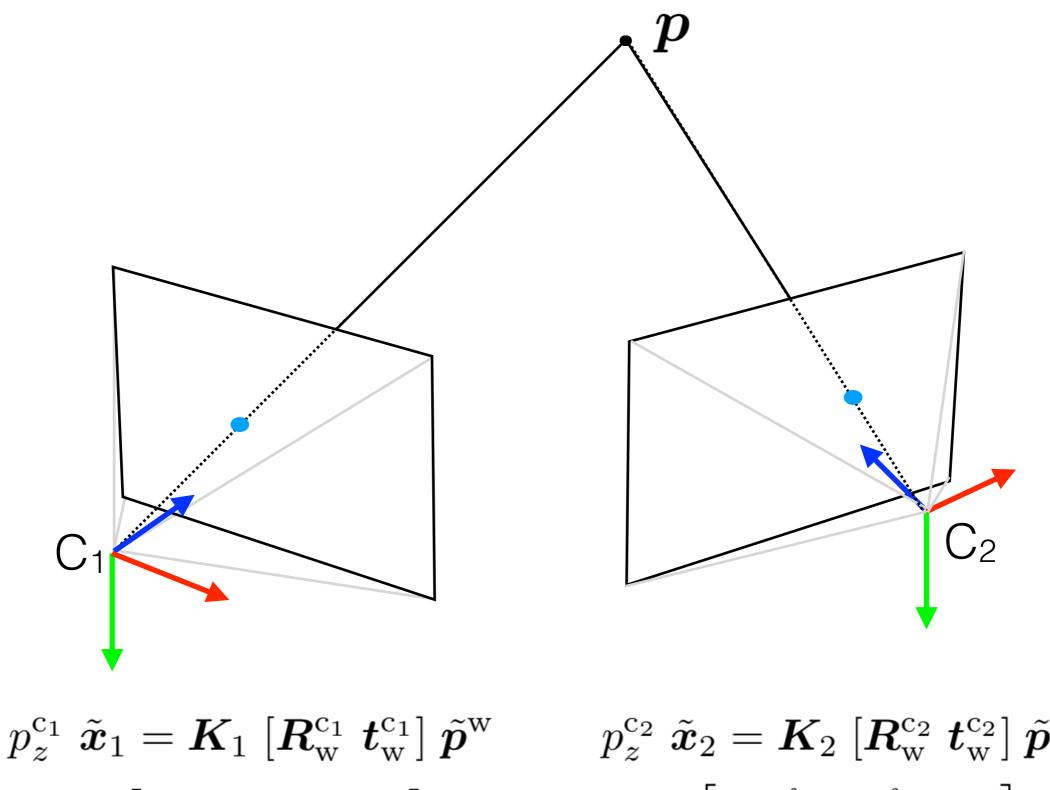


Question: can we estimate the motion of the camera between *I*₁ and *I*₂ using pixel correspondences?

Today's assumptions:

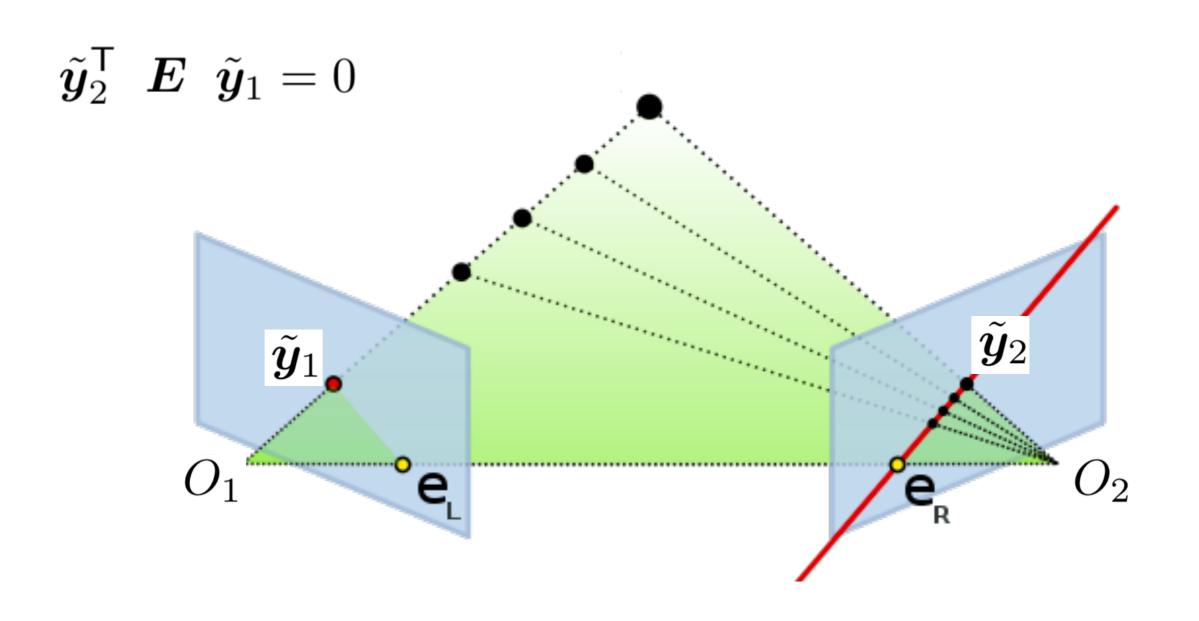
- no wrong correspondences (outliers)
- 3D point is not moving
 - camera calibration is known





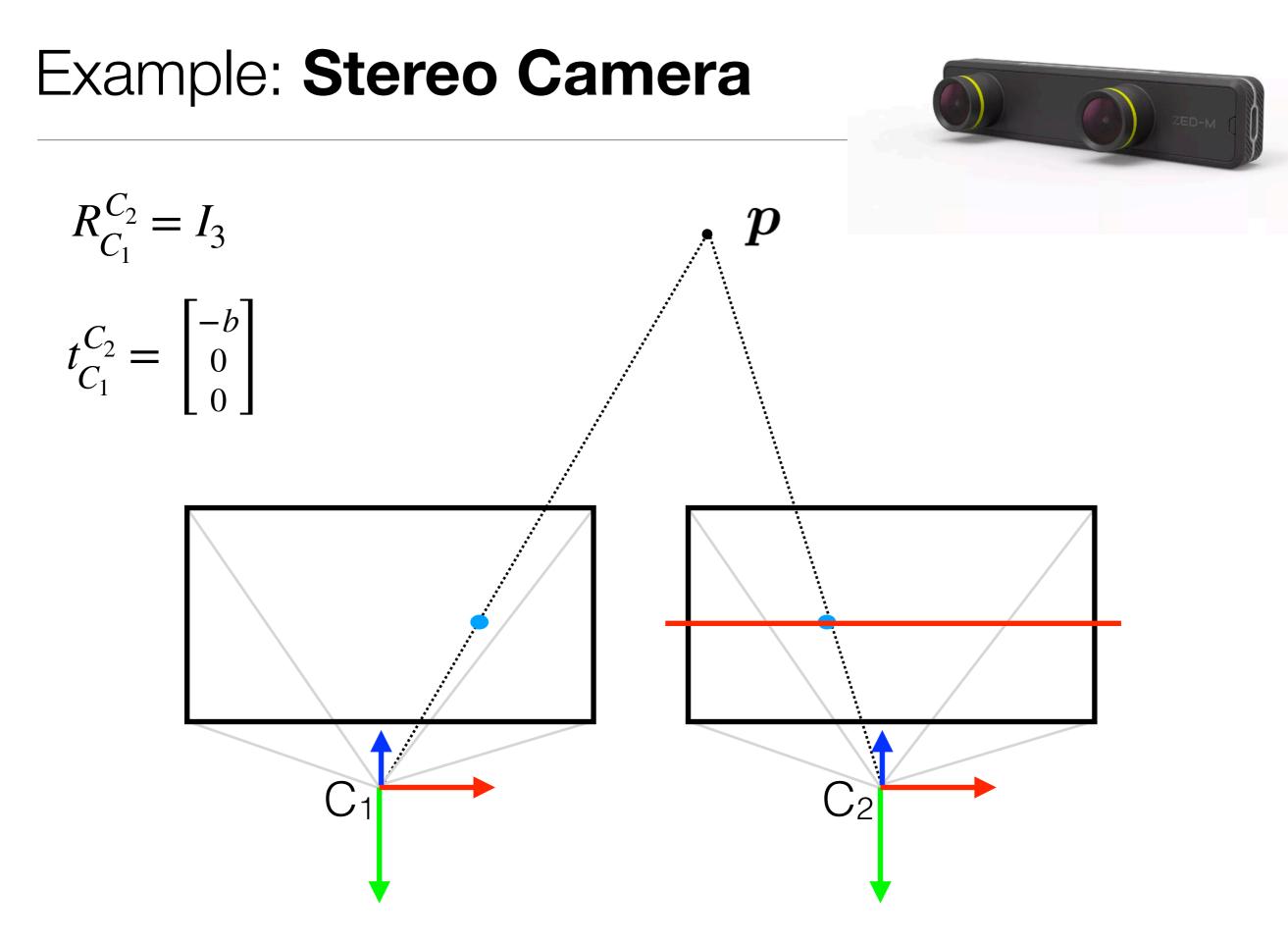
$$p_{z}^{c_{2}} \tilde{\boldsymbol{x}}_{2} = \boldsymbol{K}_{2} \begin{bmatrix} \boldsymbol{R}_{w}^{c_{2}} \boldsymbol{t}_{w}^{c_{2}} \end{bmatrix} \tilde{\boldsymbol{p}}^{w}$$
$$\boldsymbol{K}_{2} = \begin{bmatrix} s_{x_{2}} f_{2} & s_{\theta_{2}} f_{2} & o_{x_{2}} \\ 0 & s_{y_{2}} f_{2} & o_{y_{2}} \\ 0 & 0 & 1 \end{bmatrix}$$

Epipolar Geometry



epipolar plane / epipolar line

eL, eR: epipoles



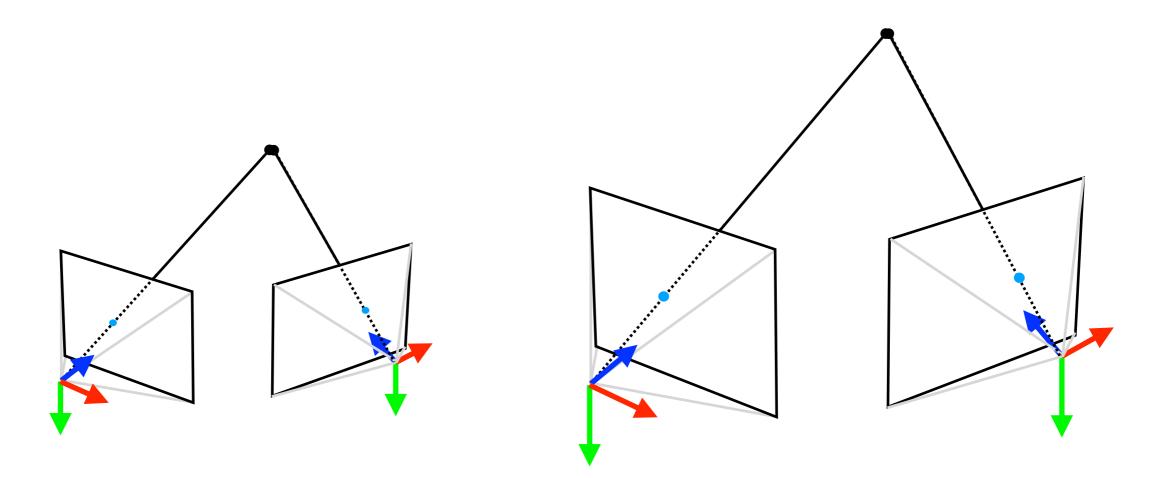
also: easy to triangulate points given geometry

Estimating Poses from Correspondences

Given N calibrated pixel correspondences:

$$(\tilde{y}_{1,k}, \tilde{y}_{2,k})$$
 for $k = 1, ..., N$

compute the relative pose between the cameras



Can we estimate the scale of the translation (baseline)?

Estimating Poses from Correspondences

Given *N* calibrated pixel correspondences:

$$(\tilde{y}_{1,k}, \tilde{y}_{2,k})$$
 for $k = 1, ..., N$

1. leverage the epipolar constraints to estimate the essential matrix *E*

 $\tilde{\boldsymbol{y}}_{2,k}^{\mathsf{T}} \boldsymbol{E} \; \tilde{\boldsymbol{y}}_{1,k} = 0$

- Retrieve the rotation and translation (up to scale) from the *E*
- $oldsymbol{E} = [oldsymbol{t}]_{ imes}oldsymbol{R}$

Retrieving Pose from Essential Matrix

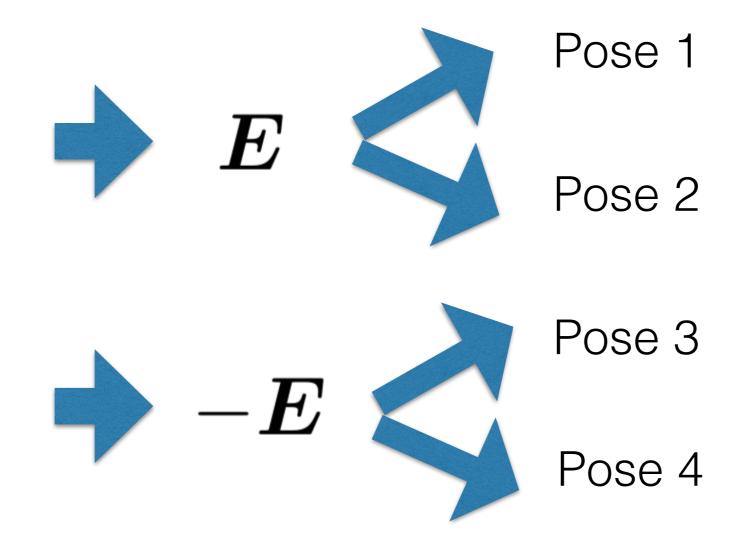
 t_2

Theorem 1 (Pose recovery from essential matrix, Thm 5.7 in [1]). There exist exactly two relative poses (\mathbf{R}, \mathbf{t}) with $\mathbf{R} \in SO(3)$ and $\mathbf{t} \in \mathbb{R}^3$ corresponding to a nonzero essential matrix \mathbf{E} (i.e., such that $\mathbf{E} = [\mathbf{t}]_{\times} \mathbf{R}$):

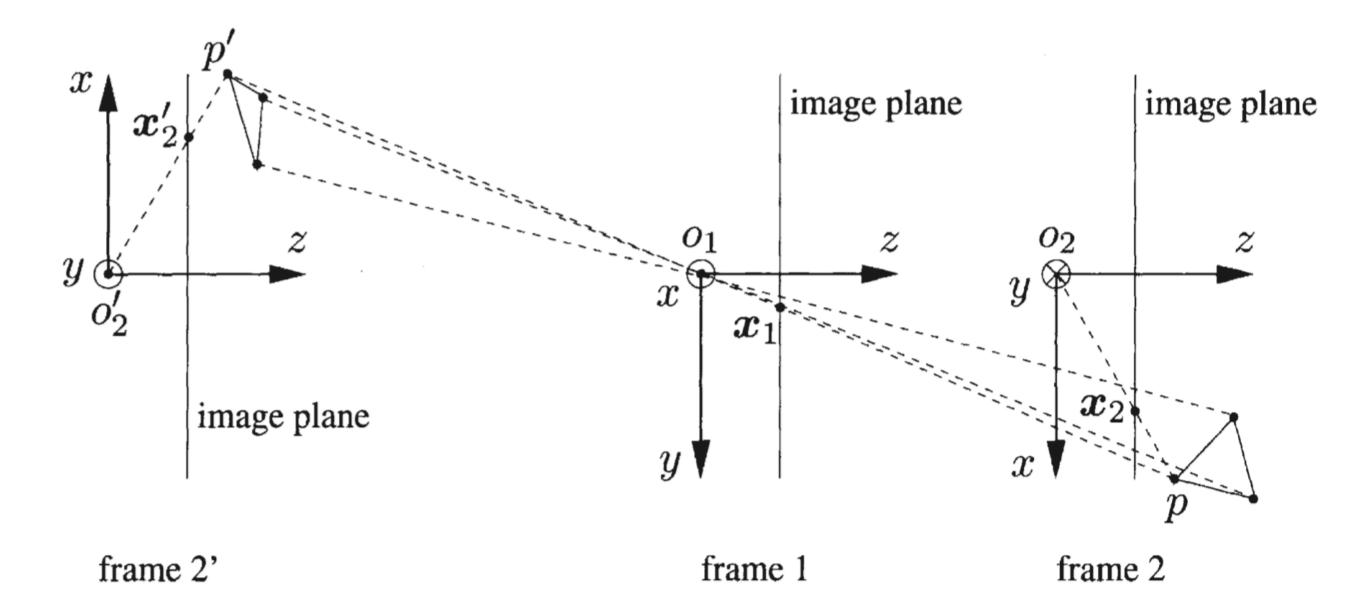
$$\boldsymbol{t}_1 = \boldsymbol{U}\boldsymbol{R}_z(+\pi/2)\boldsymbol{\Sigma}\boldsymbol{U}^{\mathsf{T}} \qquad \boldsymbol{R}_1 = \boldsymbol{U}\boldsymbol{R}_z(+\pi/2)\boldsymbol{V}^{\mathsf{T}} \qquad (13.19)$$

$$= \boldsymbol{U}\boldsymbol{R}_{z}(-\pi/2)\boldsymbol{\Sigma}\boldsymbol{U}^{\mathsf{T}} \qquad \boldsymbol{R}_{2} = \boldsymbol{U}\boldsymbol{R}_{z}(-\pi/2)\boldsymbol{V}^{\mathsf{T}} \qquad (13.20)$$

where $\mathbf{E} = \mathbf{U} \mathbf{\Sigma} \mathbf{V}^{\mathsf{T}}$ is the singular value decomposition of the matrix \mathbf{E} , and $\mathbf{R}_z(+\pi/2)$ is an elementary rotation around the z-axis of an angle $\pi/2$.



Cheirality constraints



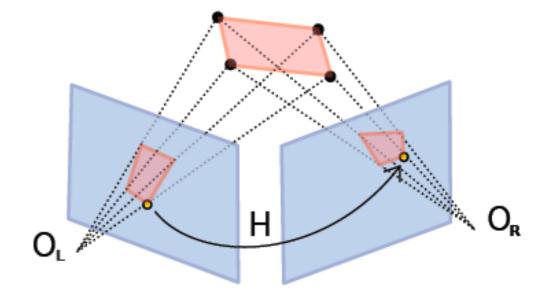
Points must be in front of the cameras!

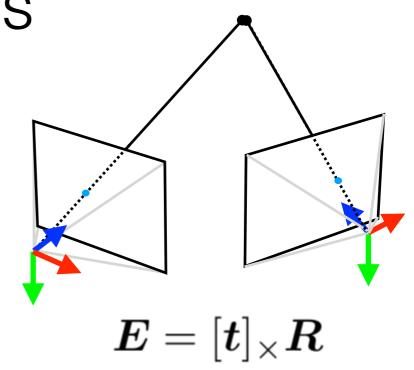
8-point method: Limitations

Number of correspondences: do we really need 8 points?

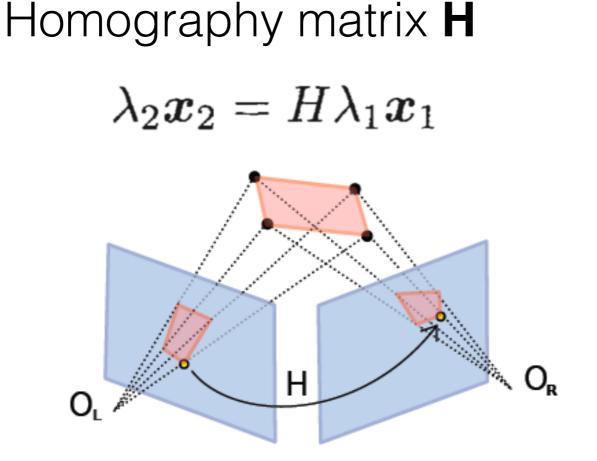
Scene structures: there are certain configurations of 3D points that make the algorithm fail

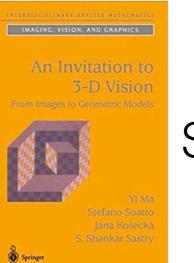
Parallax: what if *t* **= 0**?





Other Matrices in 2-view Geometry

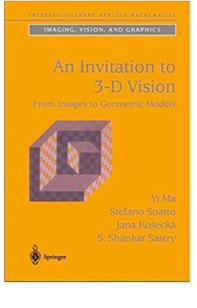




Section 5.3

Fundamental matrix **F**

$$oldsymbol{F} = oldsymbol{K}_2^{- op} ~[oldsymbol{t}]_{ imes} oldsymbol{R} ~oldsymbol{K}_1^{-1}$$



Chapter 6



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Backup

